
Programming Languages

Scheme part 1

2020

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Using Scheme interpreter

- We will run code using Chicken Scheme
- Installing on your computer:

<https://wiki.call-cc.org/platforms>

See also manual:

<http://wiki.call-cc.org/man/5/The%20User%27s%20Manual>

- Can also run online with different interpreter, works on simple examples I have tested:

<https://repl.it/languages/scheme>

Using Scheme interpreter

Using Chicken Scheme:

- Type `csi` in the terminal. It will open the chicken interpreter.
- `,q` to quit
- Chicken interpreter uses lower case for reserved words (book and some other interpreters use upper case)

Using Scheme interpreter

Our department computer also has Chicken Scheme:

- Log onto Johnston
- Then log onto one of the computers, such as wilderness etc.
- Type `csi` in the terminal. It will open the chicken interpreter

Primitive numeric functions

- Basic arithmetic: $+$, $-$, $*$, $/$
- Open csi for the following expressions

$(* 3 7)$

$(- 5 6)$

$(- 15 7 2)$

$(- 24 (* 4 3))$

$(- 24 * 4 3)$

Primitive numeric functions

- Basic arithmetic: $+$, $-$, $*$, $/$
- Open csi for the following expressions

$(-5\ 6)$

$'(-5\ 6)$

$'(-5\ 6)$

Introduction

- Other built in math functions:

modulo, round, max, min, log, sin, sqrt

(sqrt 5)

(sqrt (round 5.1))

Remember: Chicken scheme, reserved words
lower case

Lambda functions

- Nameless function:
`(lambda (x) (* x x))`
- Evaluate for parameter:
`((lambda (x) (* x x)) 3)`
- Can have multiple params:
`((lambda (a b) (+ a b)) 4 5)`
- With map:
`(map (lambda (num) (* num num num)) '(3 4 2 6))`

Define

- define used in two ways:

(1) Binds a name to a value:

```
(define pi 3.14159)
(eval pi)
```

```
(define two-pi (* 2 pi))
(eval two-pi)
```

Define

- define used in two ways:

(1) Binds a name to a value:

```
(define pi 3.14159)
(eval pi)
```

```
(define two-pi (* 2 pi))
(eval two-pi)
```

Equivalent to:

Java:

```
final float pi = 3.14159
```

```
final float two-pi = 2.0 * pi
```

Equivalent to:

C/C++:

```
const float pi = 3.14159
```

```
const float two-pi = 2.0 * pi
```

Define

- define used in two ways:

(2) Binds a name to a lambda expression:

Format:

```
(define (function_name parameters)
      (expression)
)
```

Define

- define used in two ways:

(2) Binds a name to a lambda expression:

Example:

```
(define (square number) (* number number))
```

```
(square 5)
```

```
(square 5.1)
```

Define

- define used in two ways:

(2) Binds a name to a lambda expression:

Another example: hypotenuse: length (longest side) of right triangle given two other sides

```
(define (hypotenuse side1 side2)
  (sqrt (+ (square side1) (square side2))))
)
```

```
(hypotenuse 3 4)
```

Define

- define used in two ways:

(2) Binds a name to a lambda expression:

Another example:

```
(define (hypotenuse side1 side2)
  (sqrt (+ (square side1) (square side2))))
)
```

```
(hypotenuse 3 4)
```

returns 5

Numeric predefined predicate functions

- =
- <>
- >
- <
- >=
- <=
- even?
- odd?
- zero?

Numeric predefined predicate functions

- =
- <>
- >
- <
- >=
- <=
- even?
- odd?
- zero?

Examples:

(even? 5)
(>= 7 6)

Numeric predefined predicate functions

- Two Boolean values:

#t

#f

Numeric predefined predicate functions

- Two Boolean values:

#t

#f

- Empty list evaluates as false
- Non empty list evaluates as true

Numeric predefined predicate functions

- Two Boolean values:

#t

#f

- Empty list evaluates as false
- Non-empty list evaluates as true

Similar to C integers as Boolean...

Control flow

- If expression
 1. (if predicate then_expression else_expression)

Control flow

- If expression

1. (if predicate then_expression else_expression)

Example:

Write a function for computing factorial

- Use define for defining the function name
- Use if statement for control

Control flow

- If expression

1. (if predicate then_expression else_expression)

Example:

(define (factorial n)

if statement in here...

)

Control flow

- If expression

1. (if predicate then_expression else_expression)

Example:

```
(define (factorial n)
  (if (<= n 1)
      1
      (* n (factorial (- n 1)))
  )      ;this is a comment. end if
)      ;end define
```

Control flow

- If expression

1. (if predicate then_expression else_expression)

Example:

```
(define (factorial n)
  (if (<= n 1)
      1
      (* n (factorial (- n 1)))
  )      ;this is a comment. end if
)      ;end define
```

```
(factorial 4)
```


Control flow

- If expression

1. (if predicate then_expression else_expression)

Note: We can create a file called factorial.scm with this code

```
(load "factorial.scm")  
(factorial 4)
```

Control flow

- Cond statement

2. Multiple selection via cond:

```
( cond  
  (predicate_1 expression_1)  
  (predicate_2 expression_2)  
  ...  
  (predicate_n expression_n)  
  [ (else expression_n+1) ] ;optional  
)
```

Control flow

- Cond statement

2. Multiple selection via cond:

```
( cond  
  (predicate_1 expression_1)  
  (predicate_2 expression_2)  
  ...  
  (predicate_n expression_n)  
  [ (else expression_n+1) ] ;optional  
)
```

Predicates evaluated one at a time from first line, until one evaluates to #t. The corresponding expression is then evaluated and returned. If none evaluate #t then else is evaluated and value returned...

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

Write a function (compare x y) that returns:

“ x is greater than y ” if $x > y$

“ y is greater than x ” if $y > x$

“ x and y are equal” otherwise

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (compare x y)
  (cond
    ((> x y) "x is greater than y")
    ((< x y) "y is greater than x")
    (else "x and y are equal")
  )
)
```

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (compare x y)
  (cond
    ((> x y) "x is greater than y")
    ((< x y) "y is greater than x")
    (else "x and y are equal")
  )
)
```

30 (compare 5.1 5.1)

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
  )) ;ends define and cond
```

If can be divided by 400 evenly then leap year (evaluates to #t)

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
  )) ;ends define and cond
```

If can be divided by
100 evenly then
NOT leap year
(evaluates #f)

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
) ;ends define and cond
```

Otherwise if divisible
by 4 then leap year
is #t and if not
divisible by 4 leap
year is #f

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
) ;ends define and cond
```

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
  ) ;ends define and cond
```

Returns value
of last expression
in line that evaluates
to true

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
) ;ends define and cond
```

Try leap? On 2020 and 2021

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
) ;ends define and cond
```

```
(leap? 2020)
(leap? 2021)
```

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
) ;ends define and cond
```

```
(leap? 2020)
(leap? 2021)
```

Control flow

- Cond statement

2. Multiple selection via cond:

Example:

```
(define (leap? year)
  (cond
    ((zero? (modulo year 400)) #t)
    ((zero? (modulo year 100)) #f)
    (else (zero? (modulo year 4))))
) ;ends define and cond
```

```
(leap? 2020)
(leap? 2021)
```

List functions

- Returning an element or list

(quote a)

(quote (a b c))

List functions

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(quote a)

(quote (a b c))

Abbreviation:

'a

'(a b c)

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Why the need for quote?

List functions

- Returning an element or list

(quote a)

(quote (a b c))

Abbreviation:

`'a`

`'(a b c)`

Why the need for quote?
In Scheme and some other
Functional languages, data and
code have same format. This tells
the Interpreter it is data

List functions: car, cdr

- **car** takes a list and returns first element

```
(car `(a b c))
```

```
(car `((a b) c d ))
```

```
(car `a)
```

List functions: car, cdr

- `car` takes a list and returns first element

```
(car '(a b c))
```

```
(car '((a b) c d ))
```

```
(car 'a)
```

We got an error...

List functions: car, cdr

- **car** takes a list and returns first element

(car `(a b c))

returns a

(car `((a b) c d))

returns (a b)

(car `a)

error since a is not a list

List functions: car, cdr

- **car** takes a list and returns first element

(car '(a b c))

returns a

(car '((a b) c d))

returns (a b)

(car 'a)

error since a is not a list

(car '(a))

(car '())

List functions: car, cdr

- **car** takes a list and returns first element

(car '(a b c))

returns a

(car '((a b) c d))

returns (a b)

(car 'a)

error since a is not a list

(car '(a))

returns a

(car '())

error....

List functions: car, cdr

- **cdr** takes a list and returns list after removing first element

```
(cdr '(a b c))
```

```
(cdr '((a b) c d ))
```

```
(cdr 'a)
```

```
(cdr '(a))
```

```
(cdr '())
```

List functions: car, cdr

- **cdr** takes a list and returns list after removing first element

(cdr '(a b c))

return (b c)

(cdr '((a b) c d))

returns (c d)

(cdr 'a)

error

(cdr '(a))

returns ()

(cdr '())

error

List functions: car, cdr

- car and cdr

Names carried over from IBM 704
address and decrement parts of register

Names not intuitive...

I remember a comes before d ...

List functions: car, cdr

- Define a function named `second` that returns the second element in a list, using `car` and `cdr`

List functions: car, cdr

- Define a function named `second` that returns the second element in a list, using `car` and `cdr`

```
(define (second a_list) (car (cdr a_list)))
```

```
(second '(a b c d))
```

List functions: car, cdr

- Define a function named `second` that returns the second element in a list, using `car` and `cdr`

```
(define (second a_list) (car (cdr a_list)))
```

```
(second '(a b c d))
```

Returns `b`

Other variants of car, cdr

- `(caar x)` equivalent to `(car (car x))`

Other variants of car, cdr

- (caar x) equivalent to (car (car x))

Example:

```
(caar '((a) b c d))
```

```
(car (car '((a) b c d)) )
```


Other variants of car, cdr

- (caar x) equivalent to (car (car x))

Example:

```
(caar '((a) b c d))
```

```
(car (car '((a) b c d)) )
```

Answer a

Other variants of car, cdr

- Can keep going with it...
- Any combo of a, d up to 4 legal in-between!

Other variants of car, cdr

- Can keep going with it...
- (`caddar` x) equiv to (`car (cdr (cdr (car x)))`)

Other variants of car, cdr

- Can keep going with it...
- (caddar x) equiv to (car (cdr (cdr (car x))))

Example:

```
(caddar '((a b (c) d) e))
```

Other variants of car, cdr

- Can keep going with it...
- (caddar x) equiv to (car (cdr (cdr (car x))))

Example:

```
(caddar '((a b (c) d) e))
```

Answer (c). Why?

Other variants of car, cdr

- Can keep going with it...
- (caddar x) equiv to (car (cdr (cdr (car x))))

Example:

```
(caddar '((a b (c) d) e))
```

Answer (c)

Because:

1st inner car = (a b (c) d)

Next inner cdr = (b (c) d)

Next cdr = ((c) d)

Final outer car = (c)

Creating a list

- Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with **first param as first element**, and **second param as remainder** of the result.

Creating a list

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Example: `(cons 'a '(b c))`

Returns?

Creating a list

- Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with first param as first element, and second param as remainder of the result.

Example: (cons 'a '(b c))

Returns? (a b c)

Creating a list

- Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with first param as first element, and second param as remainder of the result.

Example: (cons 'a '())

Returns?

Creating a list

- Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with first param as first element, and second param as remainder of the result.

Example: (cons 'a '())

Returns? (a)

Creating a list

- Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with first param as first element, and second param as remainder of the result.

Example: `(cons '() '(a b))`

Returns `(() a b)`

Creating a list

- Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with first param as first element, and second param as remainder of the result.

Example: `(cons '(a b) '(c d))`

Returns `((a b) c d)`

Taking a list apart

And putting it back together

- car and cdr take a list apart
- cons constructs a new list from two given parts

Taking a list apart

And putting it back together

- What does this function do to list parameter a_list?

```
(cons (car a_list) (cdr a_list))
```

Taking a list apart

And putting it back together

- What does this function do to list parameter `a_list`?

```
(cons (car a_list) (cdr a_list))
```

Answer: returns list with exact same structure as `a_list`

Taking a list apart

And putting it back together

- What does this function do to list parameter `a_list`?

```
(cons (car a_list) (cdr a_list))
```

Answer: returns list with exact same structure as `a_list`

Example:

```
(cons (car '(a b c)) (cdr '(a b c))) = (a b c)
```

Creating a list

- Two ways
- **list**: takes any number of params; returns a list with the params as elements

Creating a list

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Example: (list 'apple 'orange 'grape)

Creating a list

- Two ways
- **list**: takes any number of params; returns a list with the params as elements

Example: (list 'apple 'orange 'grape)

Answer: (apple orange grape)

Creating a list

- Two ways
- **cons** would be more tedious for generating the list (apple orange grape) ...

Try it!

Creating a list

- Two ways
- `cons` would be more tedious for generating a list (apple orange grape) ...

Example: start from the end

```
(cons 'grape '() )
```

Results in (grape)

Then would need to add orange and then apple...

Creating a list

- Two ways
- `cons` would be more tedious for generating a list (apple orange grape) ...

Example: `(cons 'apple (cons 'orange (cons 'grape '())))`

Answer: `(apple orange grape)`

Creating a list

- Two ways
- **cons** would be more tedious for generating a list (apple orange grape) ...

Example: (cons 'apple (cons 'orange (cons 'grape '())))

Answer: (apple orange grape)

Why would we still want to use this?

Creating a list

- Two ways
- **cons** would be more tedious for generating a list (apple orange grape) ...

Example: (cons 'apple (cons 'orange (cons 'grape '())))

Answer: (apple orange grape)

Why would we still want to use this?

Because of how it works with car and cdr (taking a list apart versus putting it together). We will see this later in recursions.

Creating a list

- Summary: Two ways
- **cons**: takes two params, the first either an atom or a list, and the second a list. Returns a new list with first param as first element, and second param as remainder of the result.
- **list**: takes any number of params; returns a list with the params as elements.