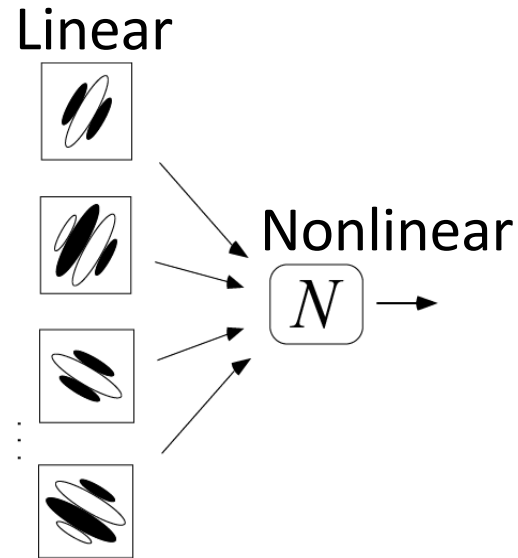


# **SPIKE TRIGGERED APPROACHES**

**Odelia Schwartz**  
**Computational Neuroscience Course 2021**

## LINEAR NONLINEAR MODELS

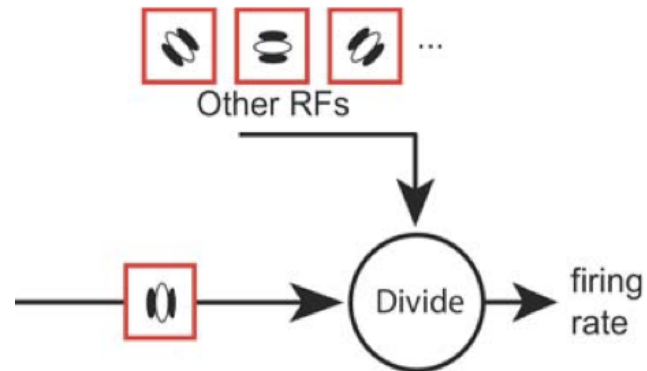


- Often constrain to some form of **Linear, Nonlinear** computations, e.g. visual receptive fields or filters, followed by nonlinear interactions

## LINEAR NONLINEAR MODELS

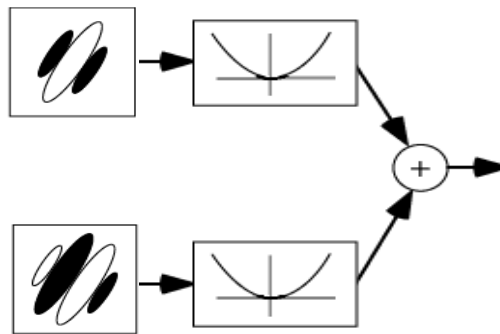
What type of nonlinearities?

## DESCRIPTIVE MODELS: DIVISIVE NORMALIZATION



- Canonical computation (Carandini, Heeger, 2013)
- Has been applied to primary visual cortex (V1)
- More broadly, to other systems and modalities, multimodal processing, value encoding, etc

## DESCRIPTIVE MODELS: COMPLEX CELLS AND INVARIANCE



- after Adelson & Bergen, 1985

## FITTING DESCRIPTIVE MODELS TO DATA

Linear



...



Nonlinear

$N$

Poisson



## ROADMAP

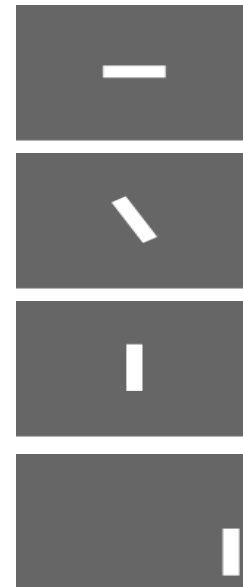
- Simple cell – traditional approach
- Simple cell (STA)
- When STA fails
- Complex cell (STC)
- Another example (STC)
- More generic model with multiple filters

## REMINDER: RECEPTIVE FIELD

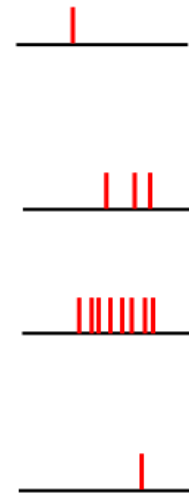
Hubel and Wiesel, 1959



Stimuli



Spikes





**REMINDER: RECEPTIVE FIELD**

Primary Visual Cortex (V1)



## RECEPTIVE FIELD

Filter



Stimulus



= Positive response

Filter



Stimulus



= Negative response

Filter



Stimulus



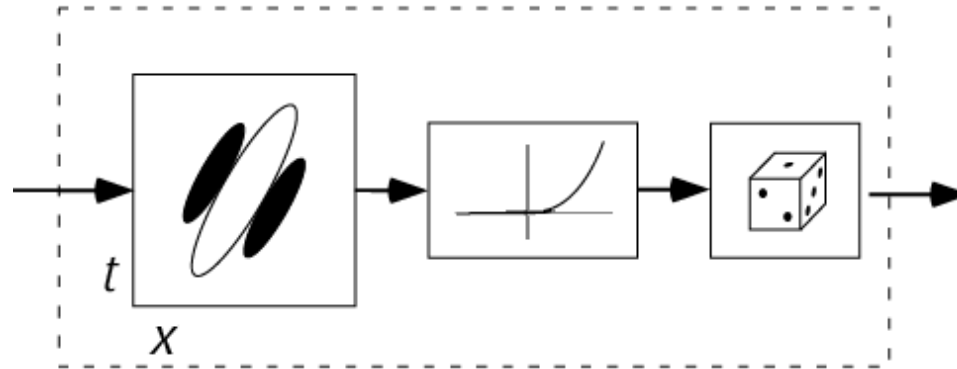
= Zero response

- Response of a filter  
= inner/dot product/projection of filter with stimulus

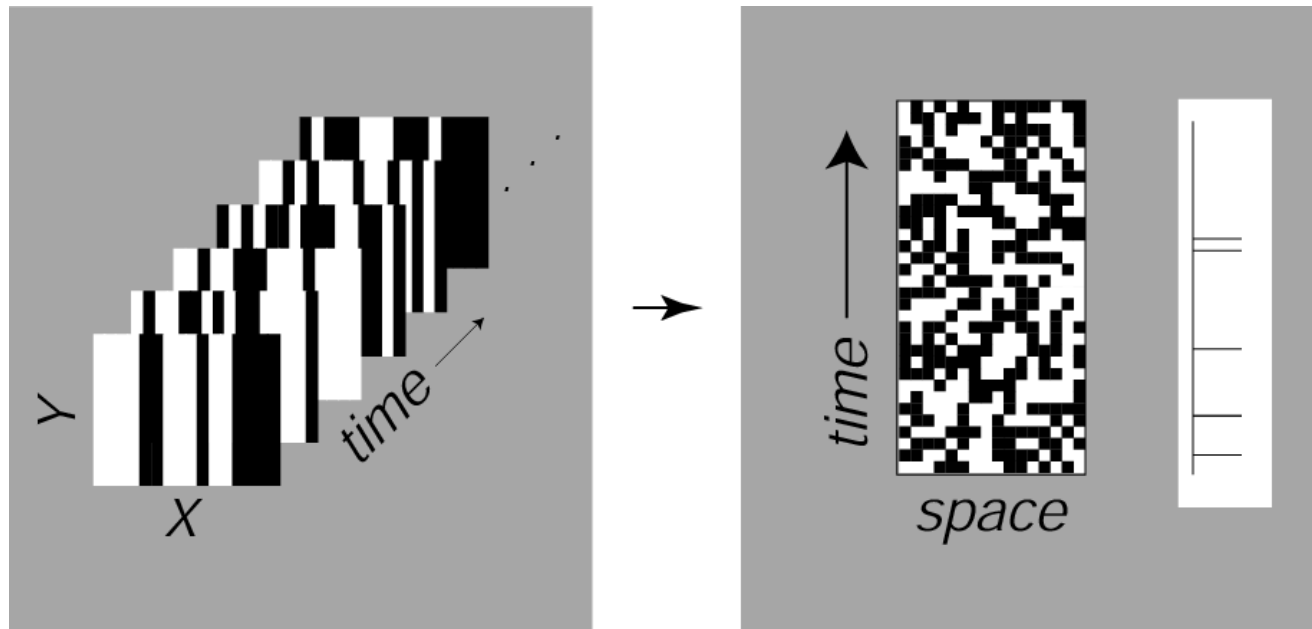
## ROADMAP

- Simple cell – traditional approach
- Simple cell (STA)
- When STA fails
- Complex cell (STC)
- Another example (STC)
- More generic model with multiple filters

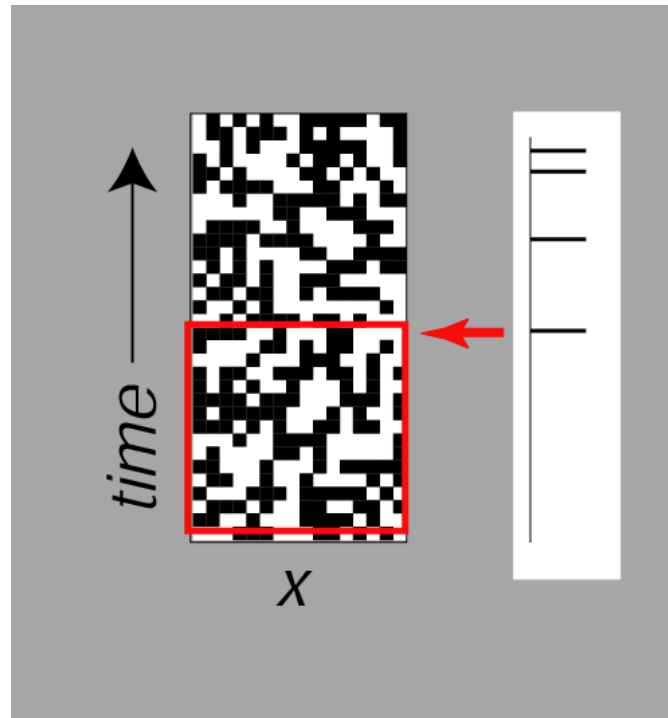
*Simple cell*



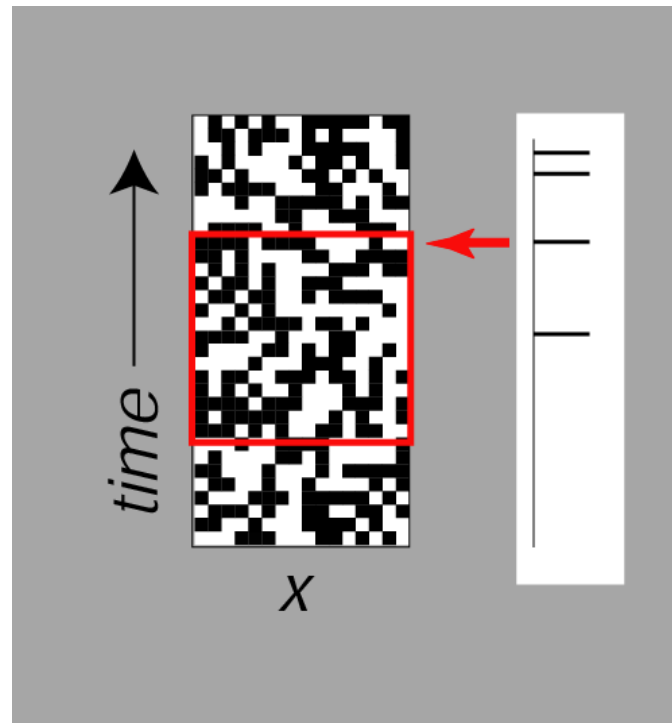
## SPIKE-TRIGGERED AVERAGE



## SPIKE-TRIGGERED AVERAGE



## SPIKE-TRIGGERED AVERAGE

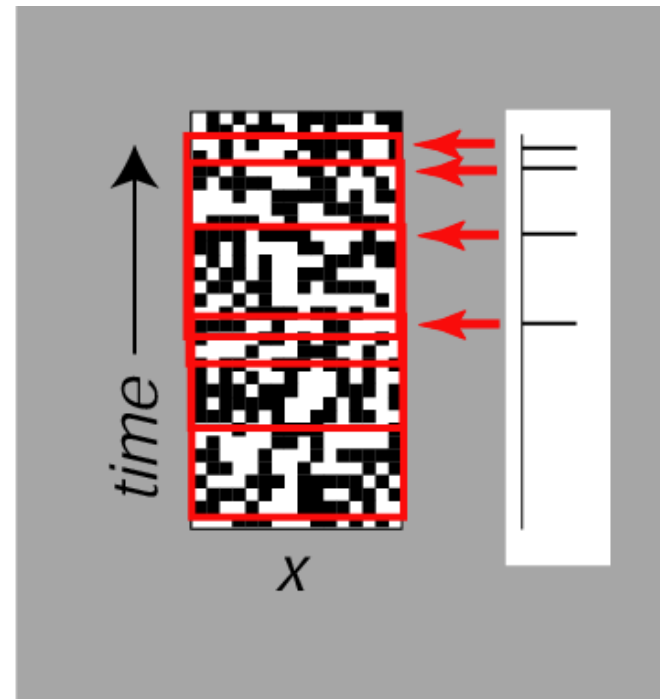


## SPIKE-TRIGGERED AVERAGE

STA

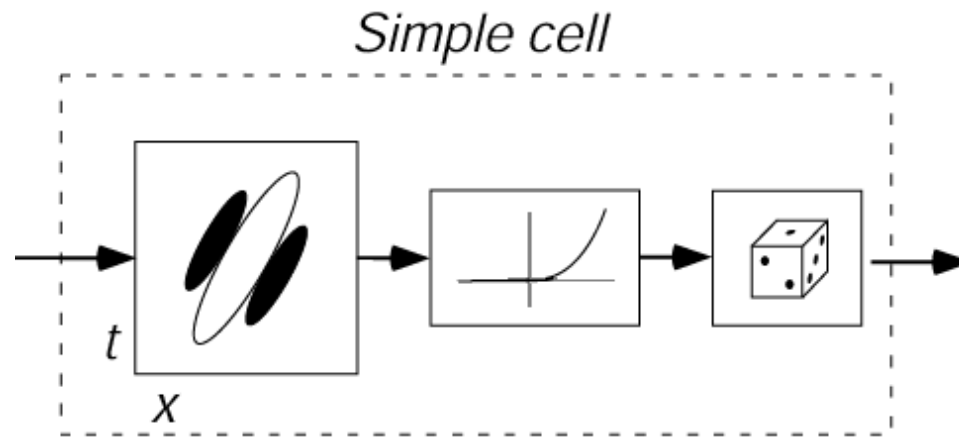


Average of  
spike-triggered  
stimuli

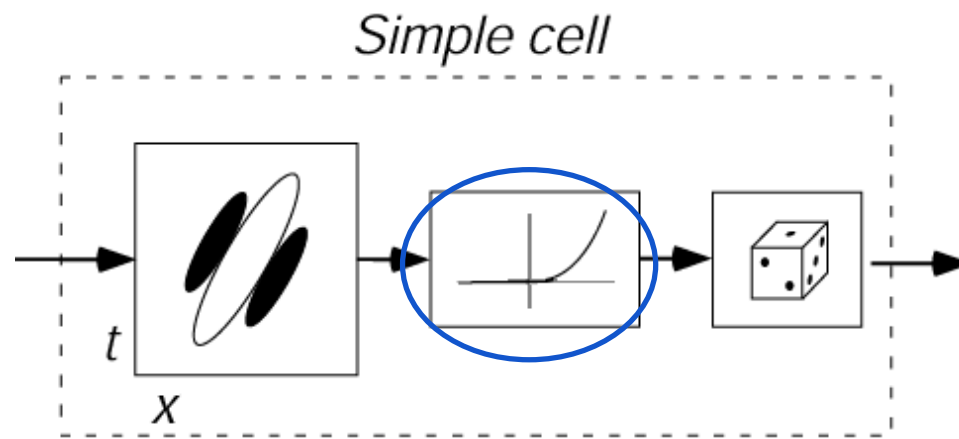




## EFFECT OF NONLINEARITY IN MODEL?



## EFFECT OF NONLINEARITY IN MODEL?



## EFFECT OF NONLINEARITY IN MODEL?

Filter



Stimulus



= Positive response



Positive

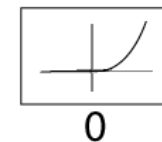
Filter



Stimulus



= Negative response



Zero

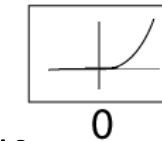
Filter



Stimulus



= Zero response

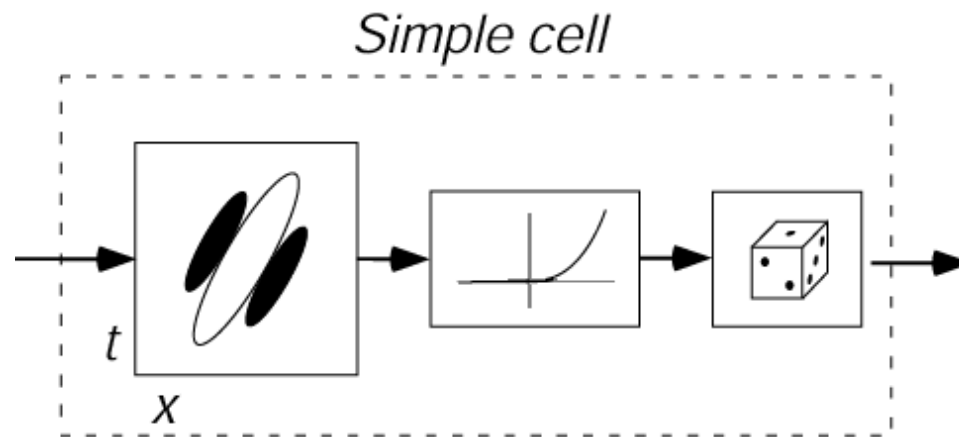


Zero

Asymmetric  
nonlinearity

- Nonlinearity sets negative filter responses to zero (firing rates are positive)

## SPIKE-TRIGGERED AVERAGE (STA)

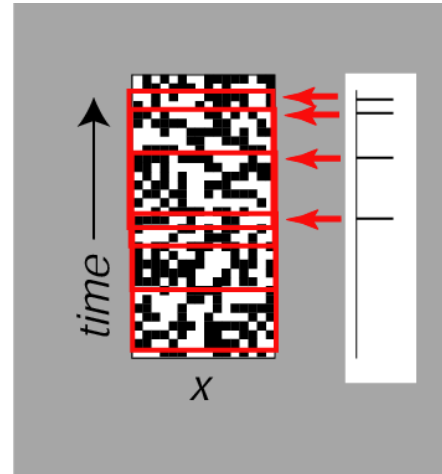


- Stimuli that are more similar to filter are more likely to elicit a spike...

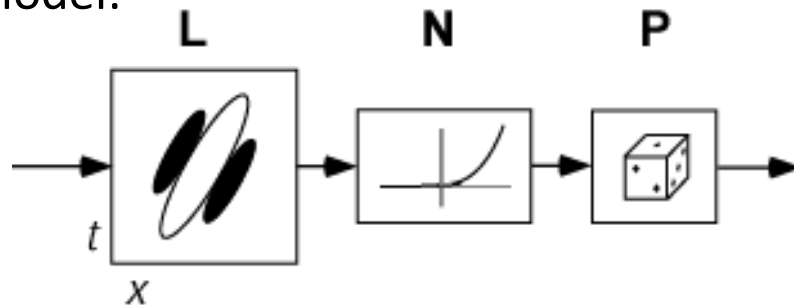
## SPIKE-TRIGGERED AVERAGE (STA)



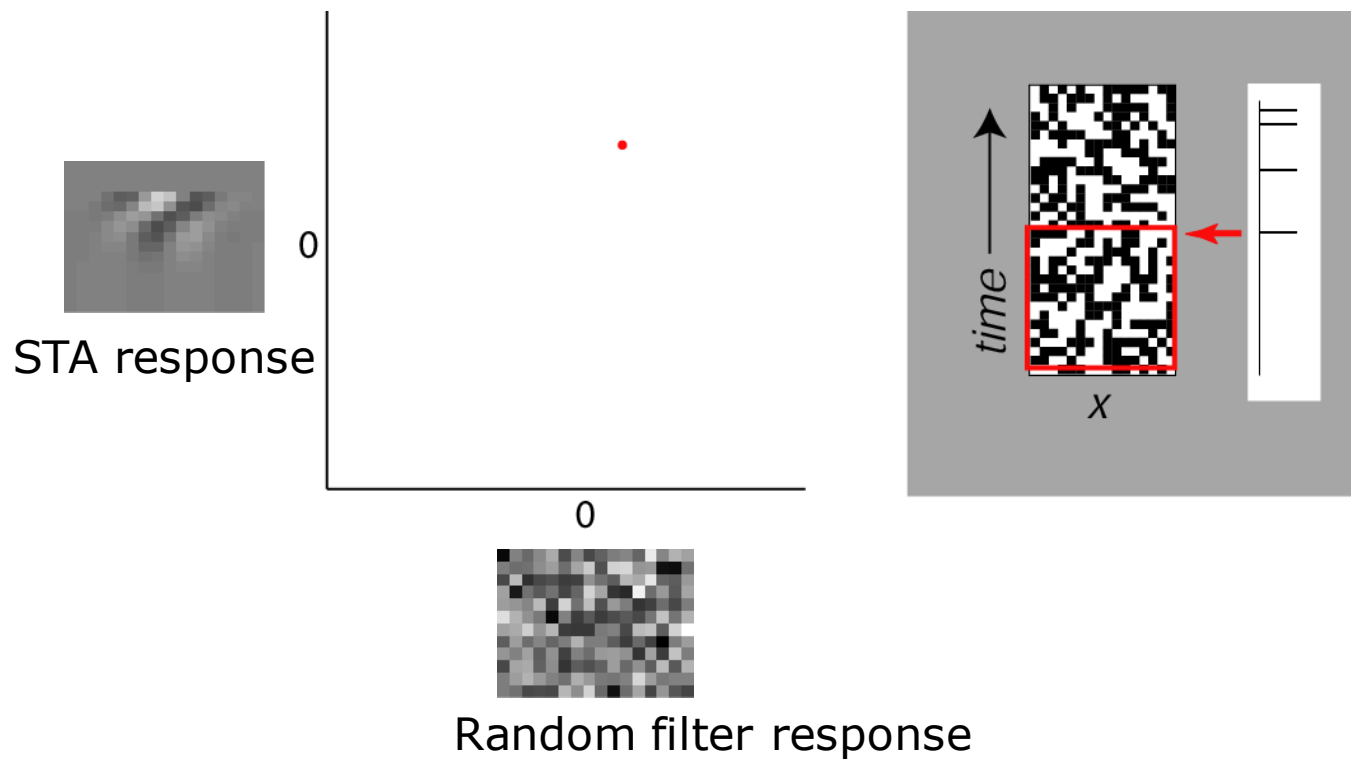
Average of  
spike-triggered  
stimuli



Model:

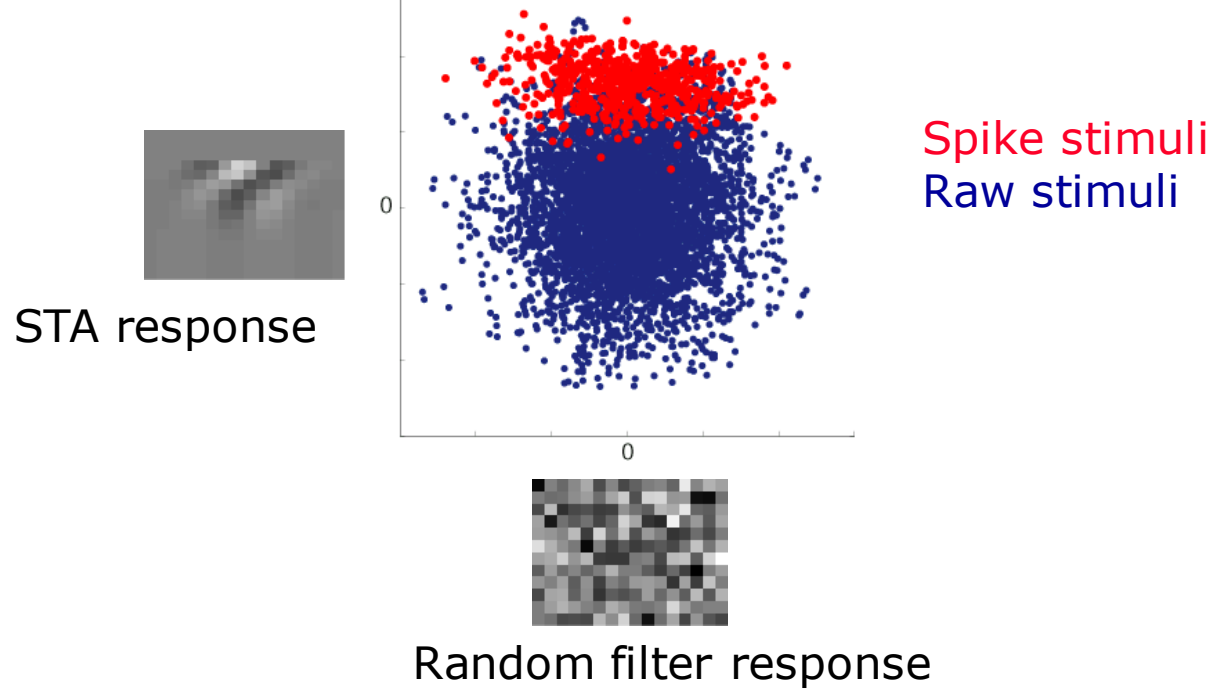


## SPIKE-TRIGGERED AVERAGE (STA)



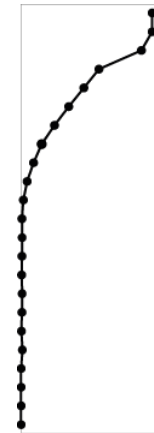
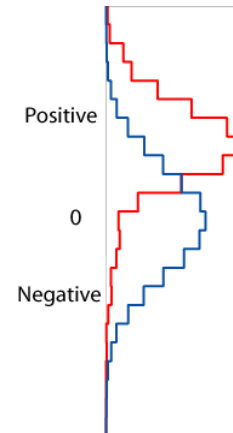
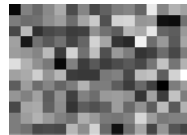
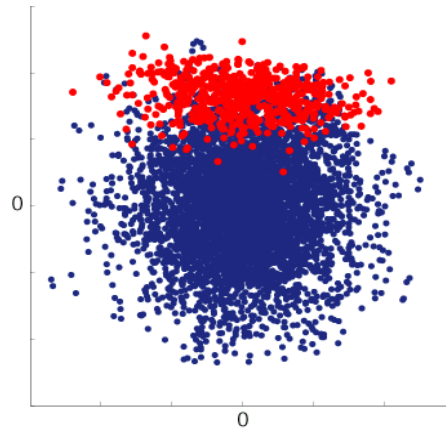
## SPIKE-TRIGGERED AVERAGE (STA)

**Geometrical view: change in the mean**  
Large filter response likely to elicit spike



## SPIKE-TRIGGERED AVERAGE (STA)

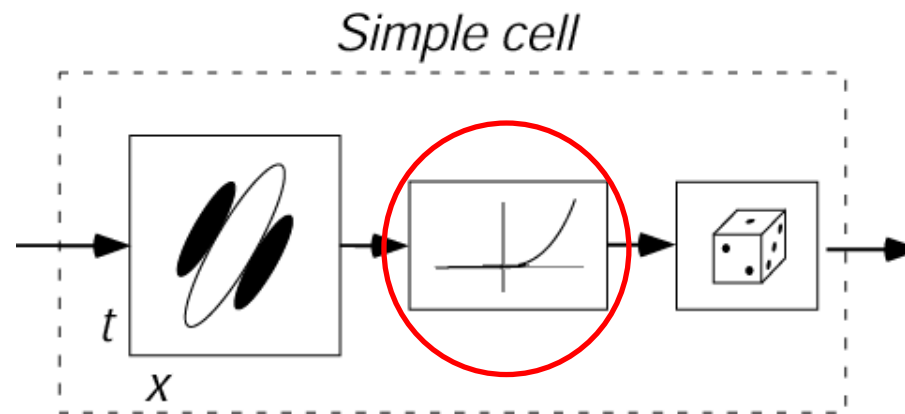
STA



**We can also recover the nonlinearity**



## SPIKE-TRIGGERED AVERAGE (STA)



**We can also recover the nonlinearity**

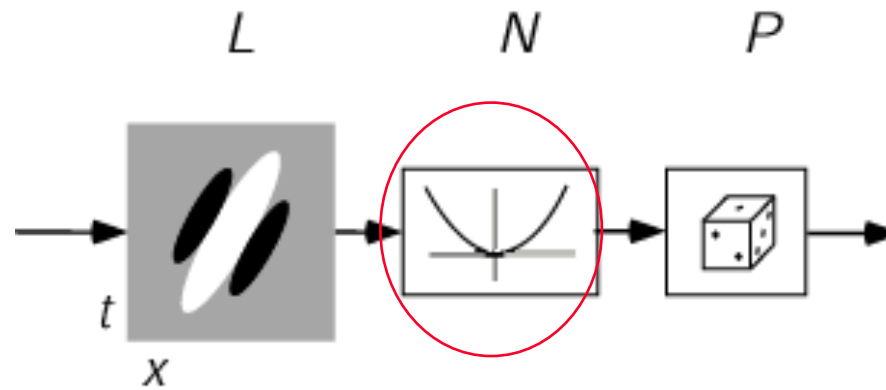
## STEPS

1. Assume a model (filter/s, nonlinearity)  
(we assumed one filter and asymmetric nonlinearity)
2. Estimate model components (filter/s, nonlinearity)  
(we looked for changes in mean: STA)

## ROADMAP

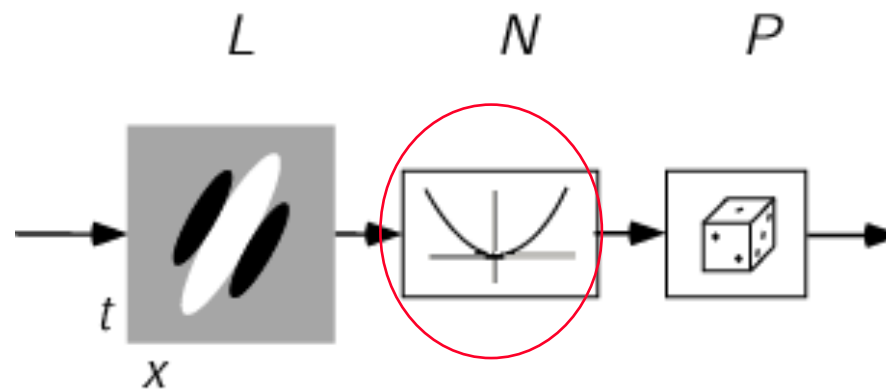
- Simple cell – traditional approach
- Simple cell (STA)
- **When STA fails**
- Complex cell (STC)
- Another example (STC)
- More generic model with multiple filters

**BUT STA DOES NOT ALWAYS WORK**



**STA filter??**

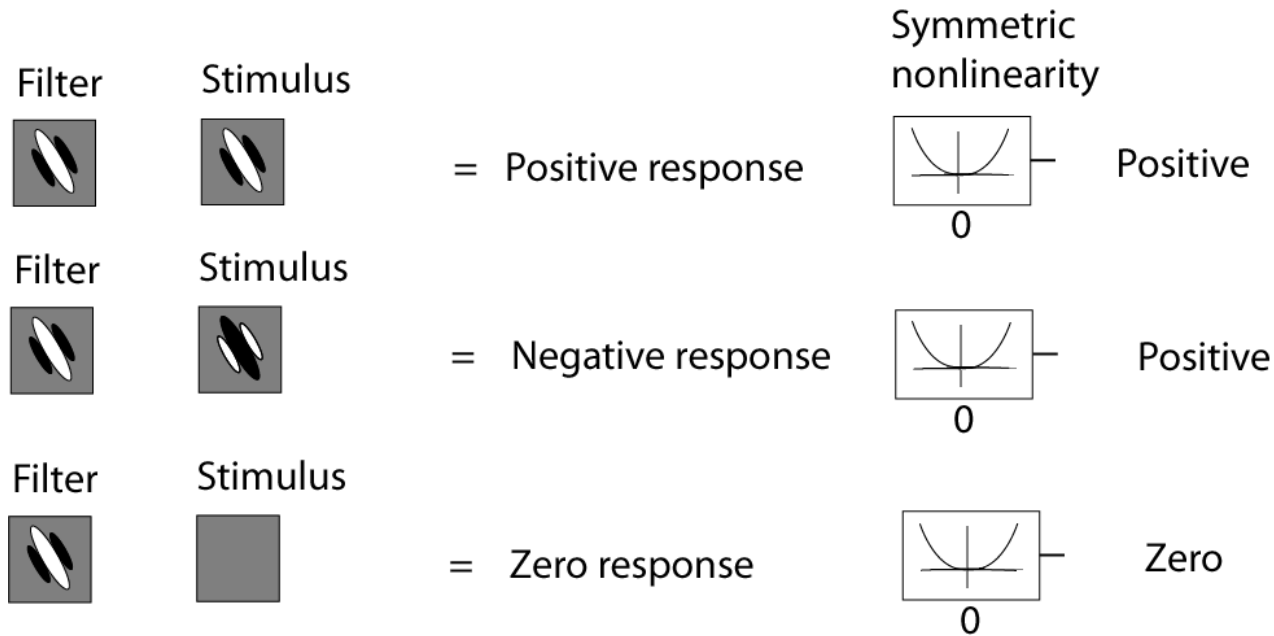
## BUT STA DOES NOT ALWAYS WORK



STA filter!

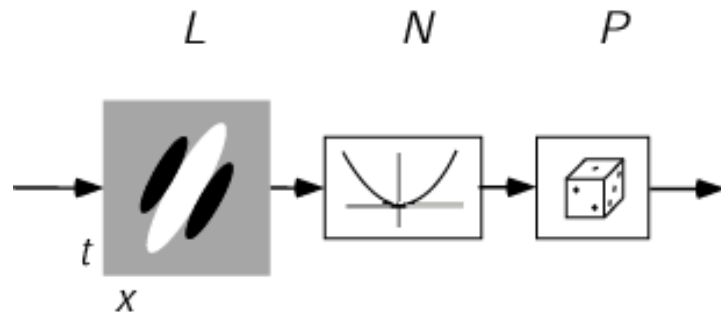


## WHAT HAPPENED??

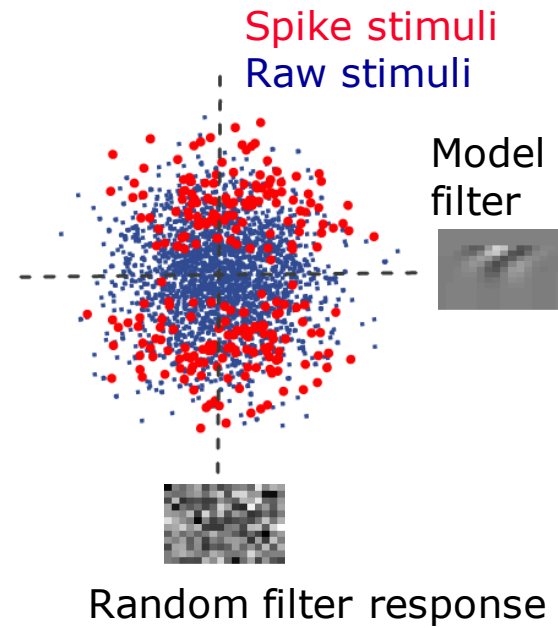


**Nonlinearity sets negative filter responses to positive  
(firing rates are positive)**

## WHAT HAPPENED??

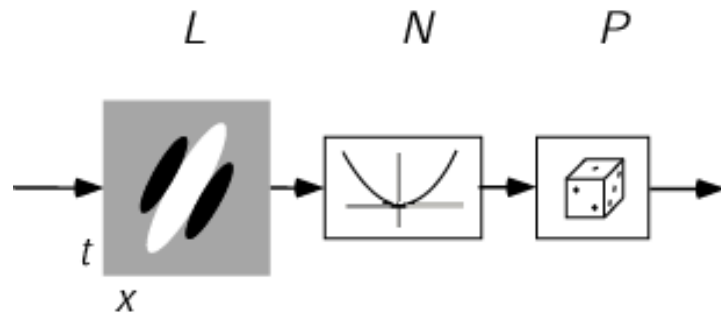


**STA filter!**

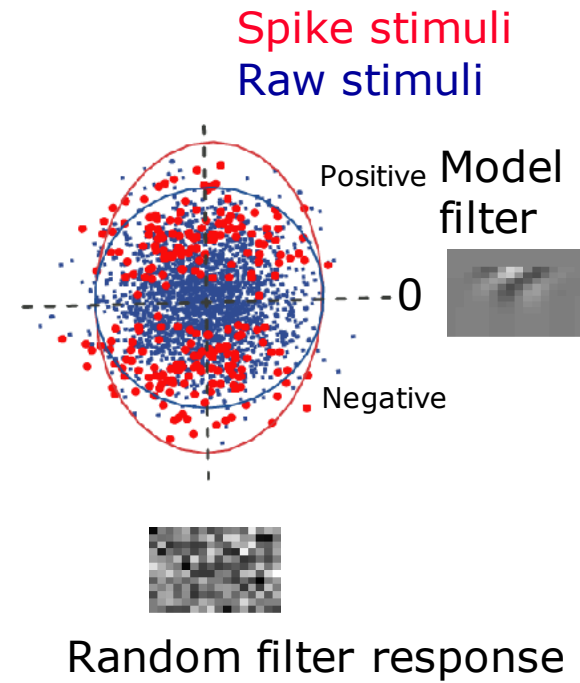


**Large or small filter response likely to elicit spike**  
**Mean stimuli eliciting spikes = 0**

## CHANGE IN THE VARIANCE



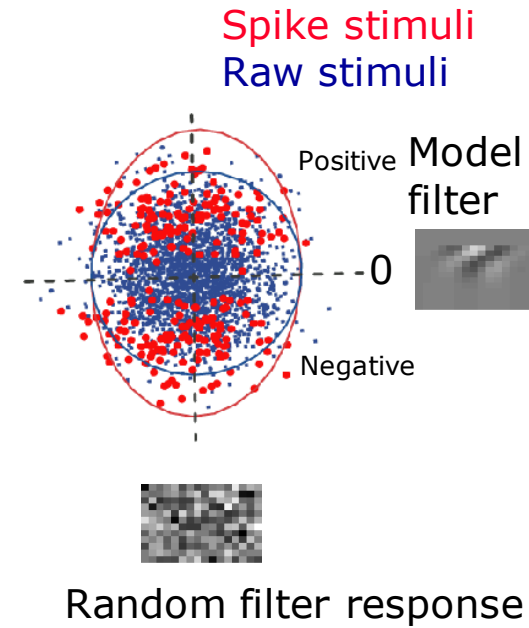
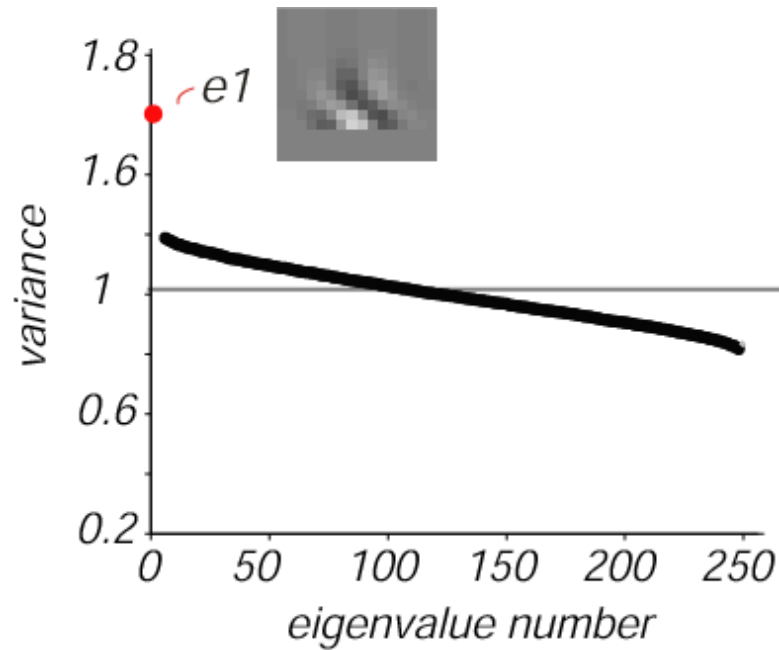
**STA filter!**



Large or small filter response likely to elicit spike

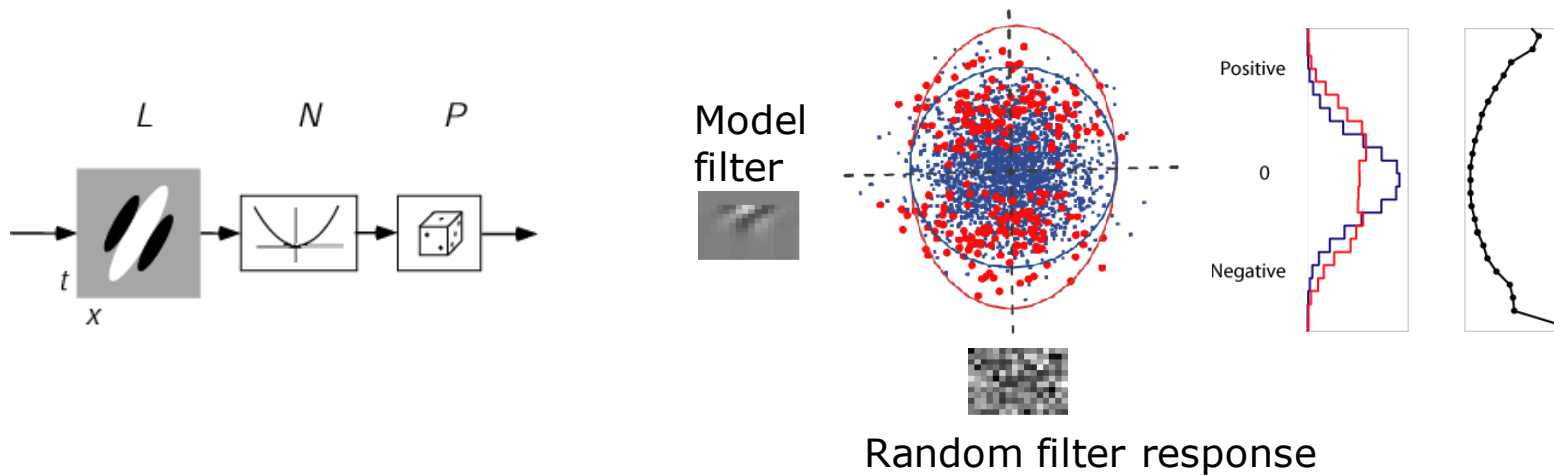


## SPIKE-TRIGGERED COVARIANCE (STC)



Standard algebra techniques (eigenvector analysis)  
recovers changes in variance

## SPIKE-TRIGGERED COVARIANCE (STC)

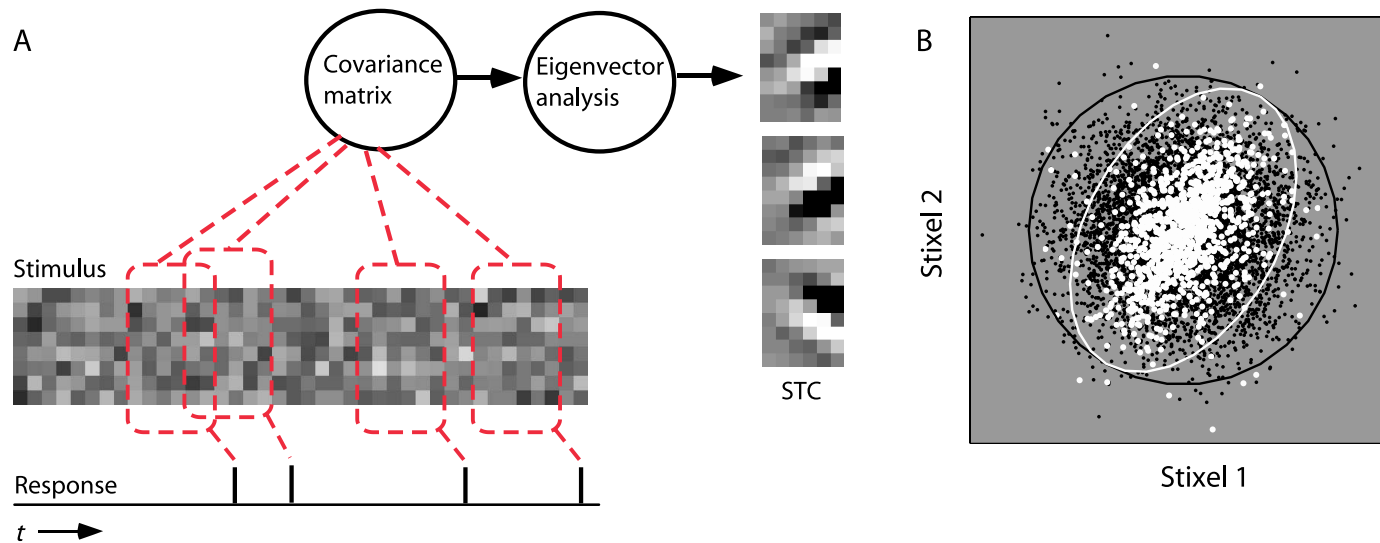


We can also recover the nonlinearity

## STEPS

1. Assume a model (filter/s, nonlinearity)  
(we assumed one filter and symmetric nonlinearity)
2. Estimate model components (filter/s, nonlinearity)  
(STA failed)  
(we looked for changes in variance: STC)

## SPIKE-TRIGGERED COVARIANCE (STC)

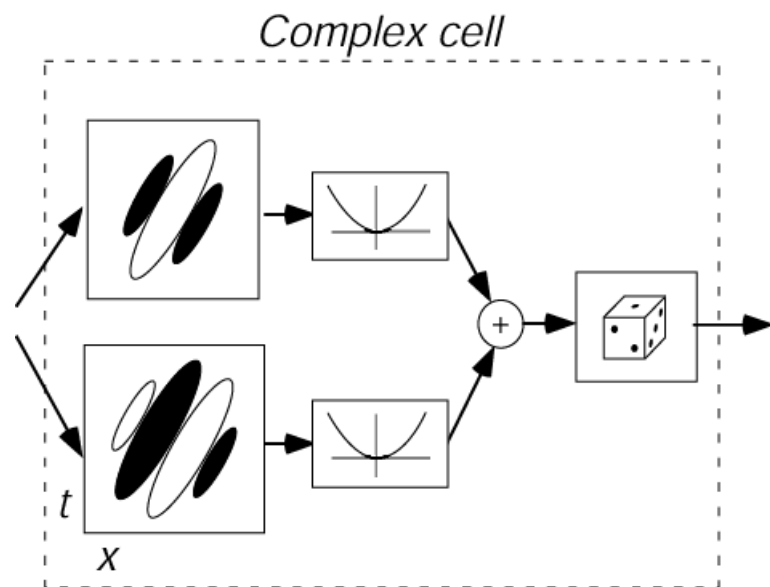


- Figure from Schwartz et al. 2006; see also Rust et al. 2005, de Ruyter & Bialek 1988
- Approach estimates linear subspace and nonlinearity
- (stixel = space time pixel)

## ROADMAP

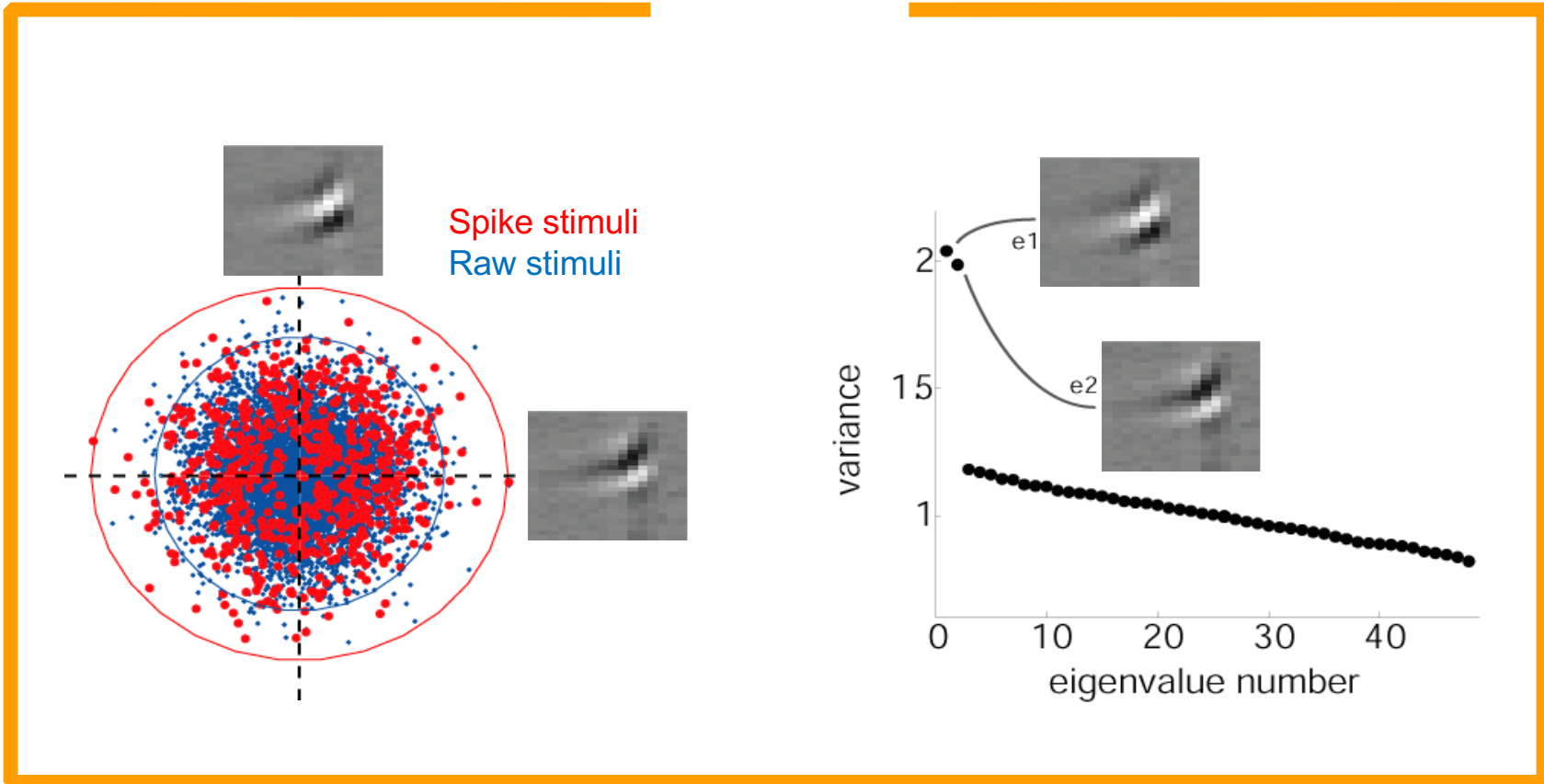
- Simple cell – traditional approach
- Simple cell (STA)
- When STA fails
- **Complex cell (STC)**
- Another example (STC)
- More generic model with multiple filters

## SPIKE-TRIGGERED COVARIANCE (STC)

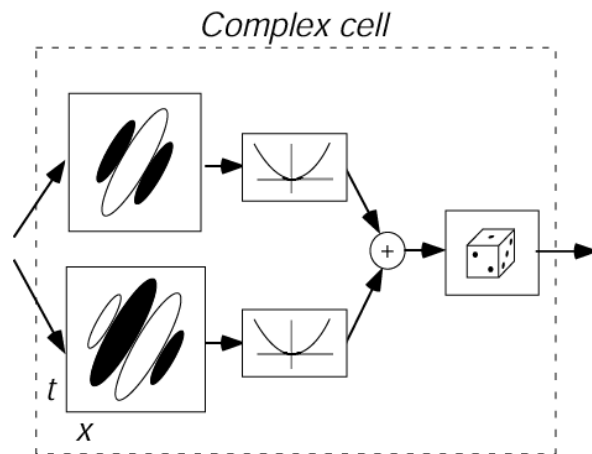


*Adelson & Bergen (1985)*

## CHANGE IN VARIANCE (STC)



## CHANGE IN VARIANCE (STC)



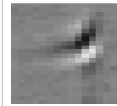
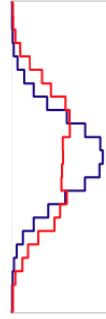
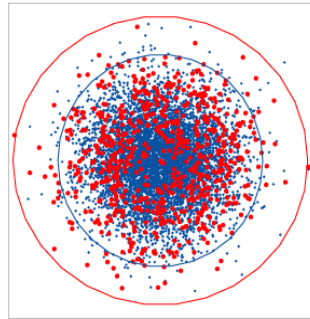
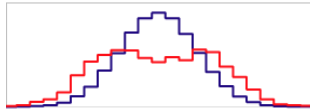
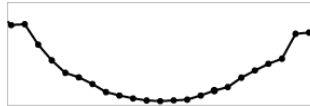
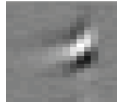
*Adelson & Bergen (1985)*

STA filter!





## CHANGE IN VARIANCE (STC)



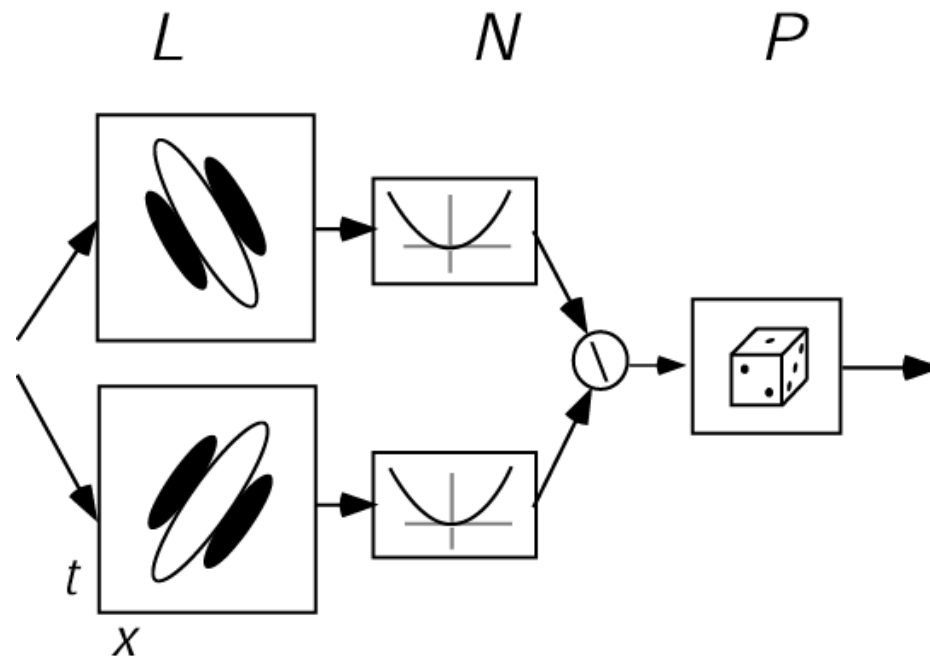
## STEPS

1. Assume a model (filter/s, nonlinearity)  
(we assumed more than one filter and symmetric nonlinearity)
2. Estimate model components (filter/s, nonlinearity)  
(STA failed)  
(we looked for changes in variance: STC)

## ROADMAP

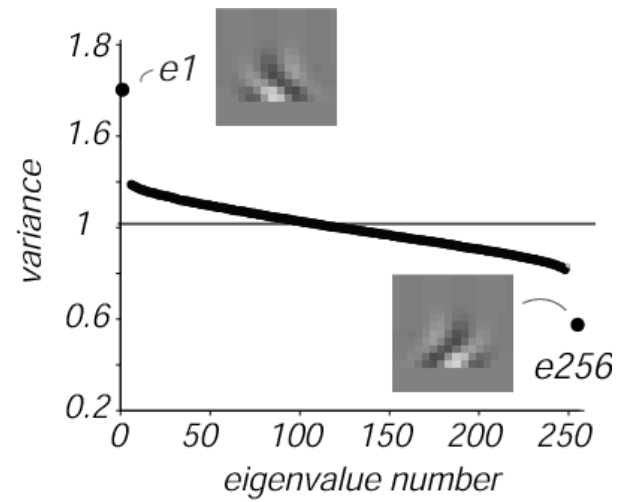
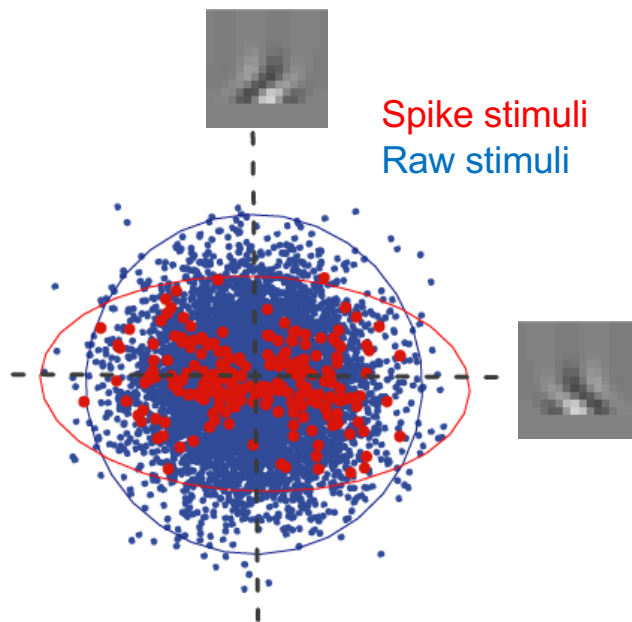
- Simple cell – traditional approach
- Simple cell (STA)
- When STA fails
- Complex cell (STC)
- **Another example (STC)**
- More generic model with multiple filters

## SECOND FILTER SUPPRESSIVE (E.G., DIVISIVE)



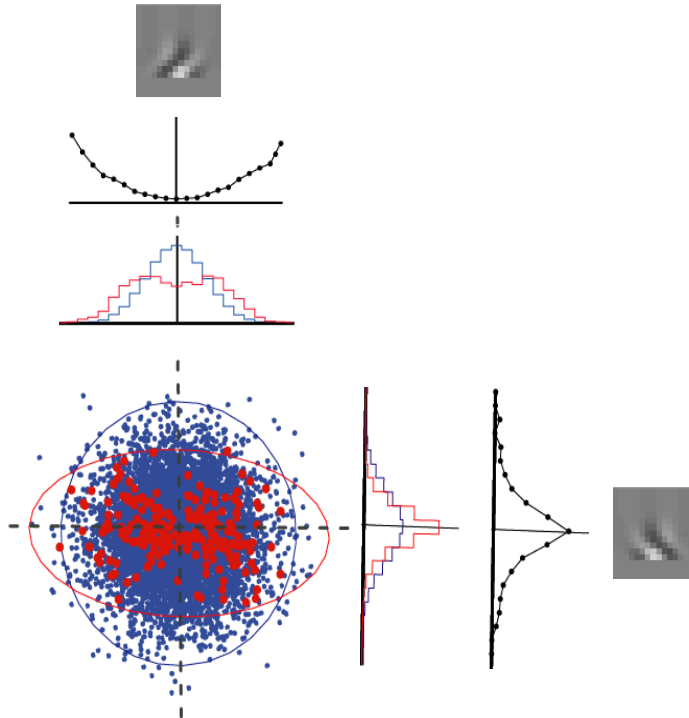
## SECOND FILTER SUPPRESSIVE (E.G., DIVISIVE)

Second filter brings about reduction in variance!



## SECOND FILTER SUPPRESSIVE (E.G., DIVISIVE)

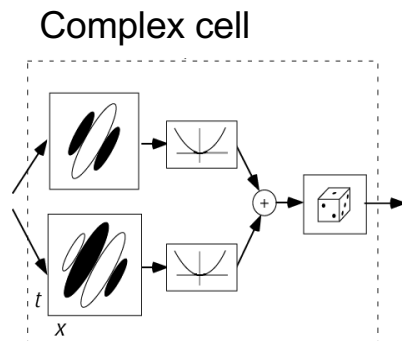
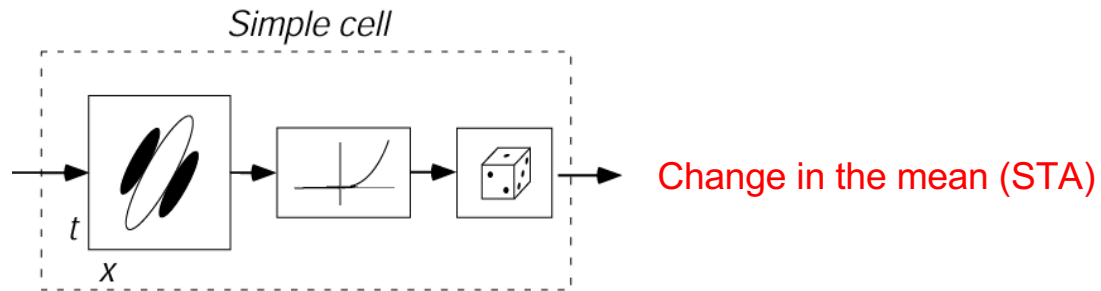
Second filter brings about reduction in variance!



## STEPS

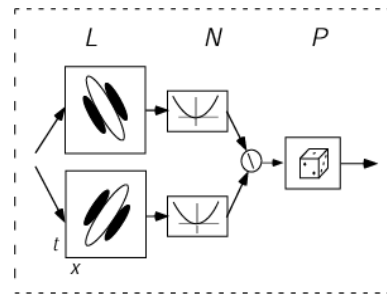
1. Assume a model (filter/s, nonlinearity)  
(we assumed more than one filter and symmetric nonlinearity)
2. Estimate model components (filter/s, nonlinearity)  
(we looked for changes in variance, this time reduced variance: STC)

## SPIKE TRIGGERED APPROACHES



*Adelson & Bergen (1985)*

### Divisive normalization



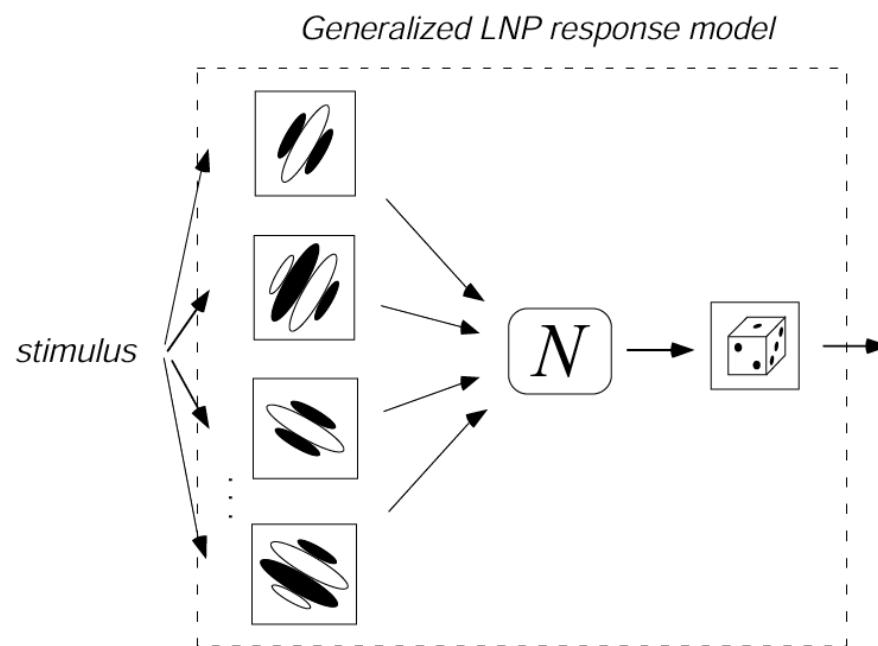


## ROADMAP

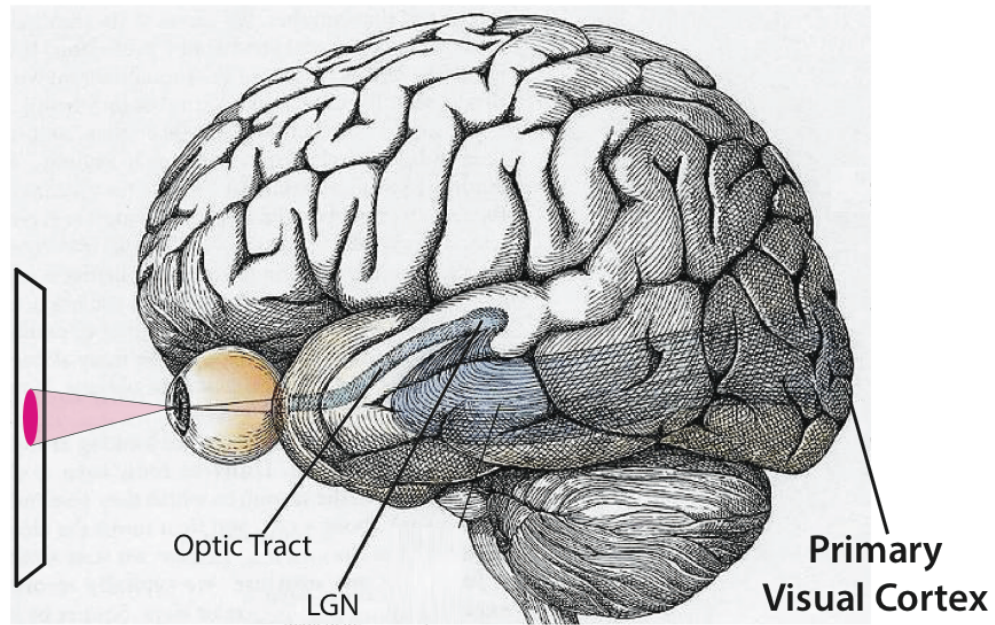
- Simple cell – traditional approach
- Simple cell (STA)
- When STA fails
- Complex cell (STC)
- Another example (STC)
- More generic model with multiple filters

## MORE GENERAL CLASS OF MODEL

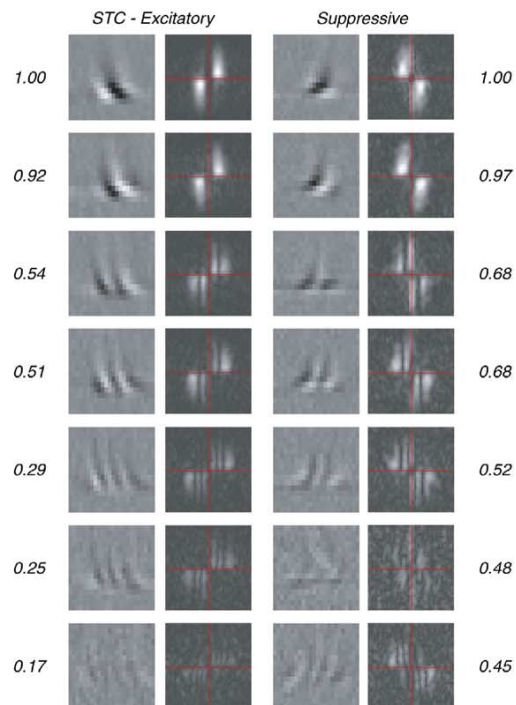
Look for changes in both the mean and the variance...



## APPLICATION: V1 EXPERIMENT

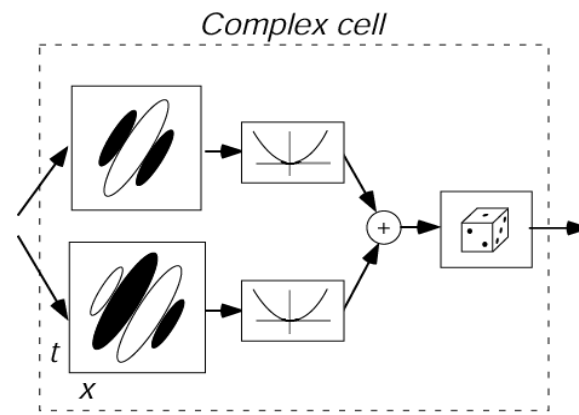
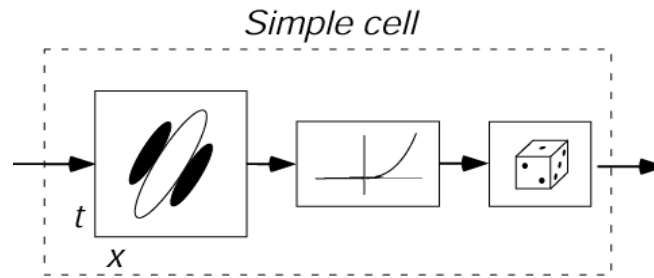


## V1 NEURAL DATA: SPIKE-TRIGGERED COVARIANCE



- Example V1 neuron estimated filters from Rust et al. 2005

## V1 NEURAL DATA: RECALL THE STANDARD MODELS



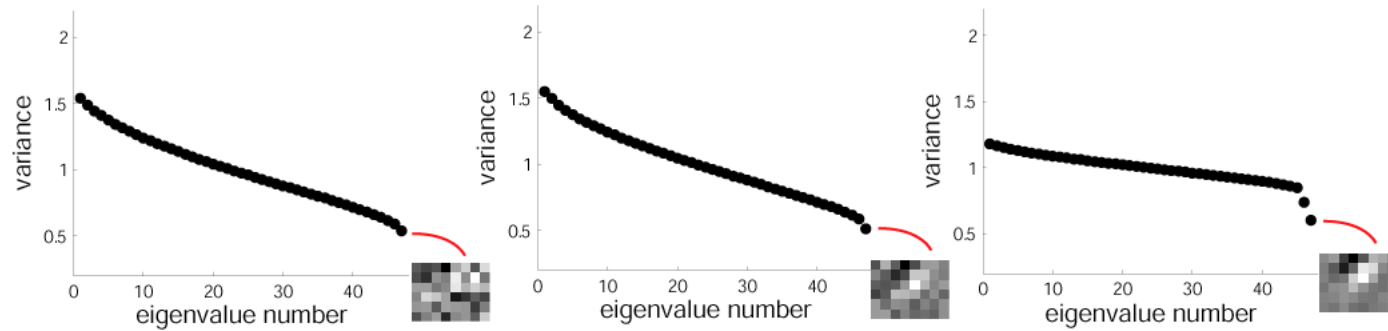
*Adelson & Bergen (1985)*

But...

Data show multiple filters (excitatory and suppressive) for both.

Are these really two different classes of neurons, or is there a continuum??

## STC ISSUES: HOW MANY SPIKES?

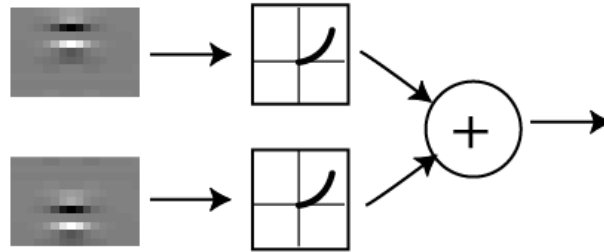


Filter estimate depends on:

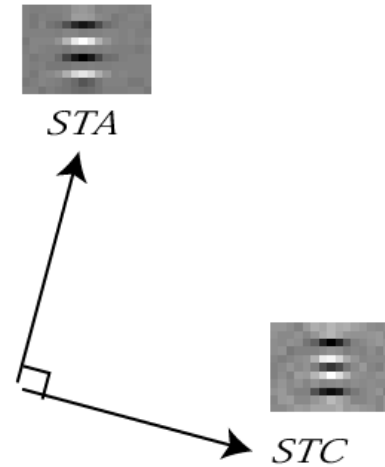
- Spatial and time dimensionality of input stimulus (smaller = better estimate)
- Number of spikes (more = better estimate)

## STC CAVEATS

Model neuron:



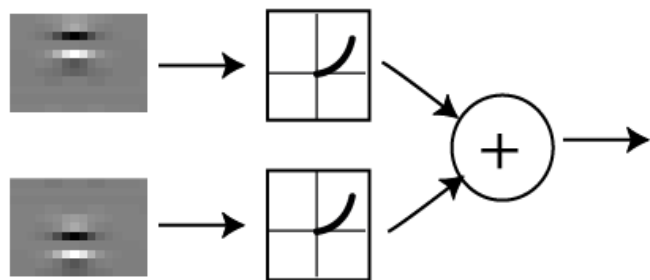
Analysis:



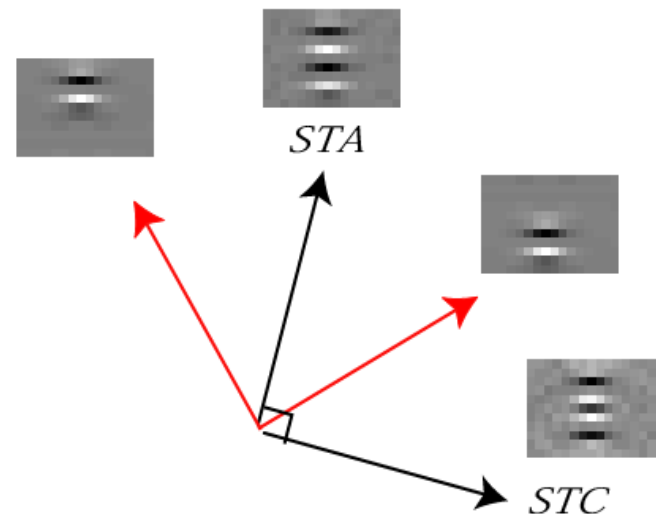
- Analysis forces filters that are 90 degrees apart!  
Filters should not be taken literally as physiological mechanisms

## STC CAVEATS

Model neuron:



Analysis:



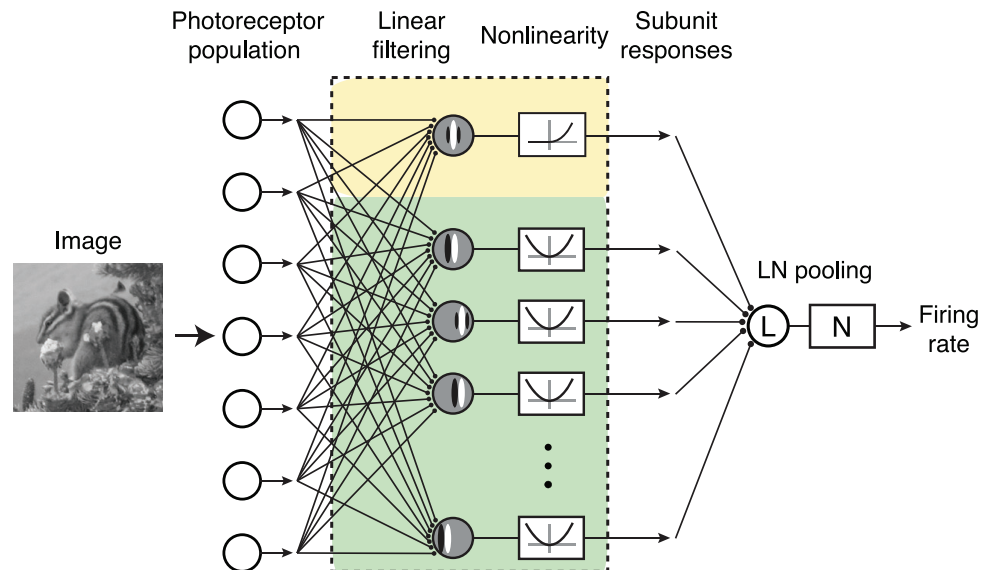
- But true filters are linear combinations of original (“span the same subspace”)



## STC CAVEATS

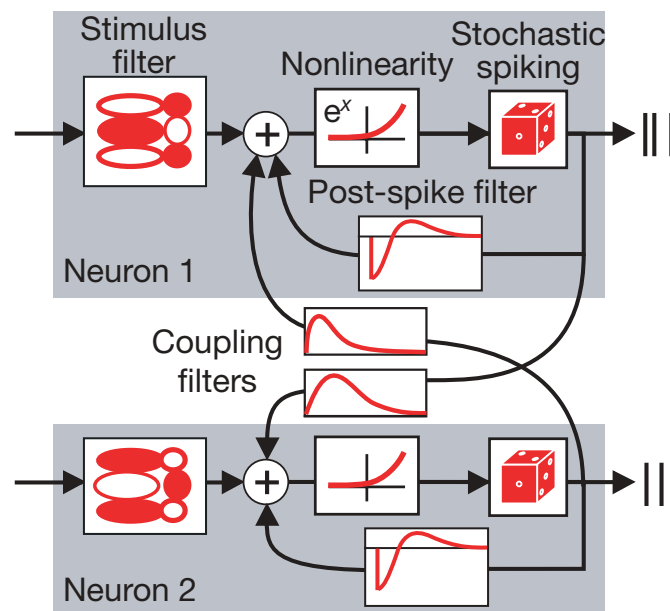
- Analysis forces filters that are 90 degrees apart!  
Filters should not be taken literally as physiological mechanisms
- Spiking in neuron may be non Poisson (bursts; refractory period; etc.)  
Filters should not be taken literally as physiological mechanisms
- There might be more filters affecting neural response than what analysis finds
- STC guaranteed to work only for Gaussian stimuli
- There might be changes that are not in the mean or variance (other approaches; e.g., info theory)

## EXAMPLE: FITTING LN-LN MODEL



- Figure from Pagan et al. 2015 describing retina and V1 with subunits (see Rust et al. 2005; Vintch et al. 2015)
- In Pagan et al. 2015 addressing higher level brain areas
- See also Rowekamp et al. 2017 addressing area V2

## EXAMPLE: GENERALIZED LINEAR MODEL



- Figure from Pillow et al., 2008, describing retina